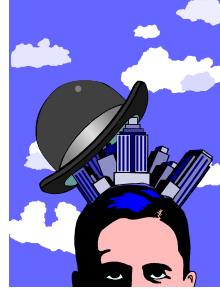


## Syllogistic Reasoning Errors

- Atmosphere Effects
  - Superficial Processing
- Conversion Effects
  - Comprehension Problems
- Belief Bias
  - Intrusion of Prior Beliefs
- Figural Effects
  - Findings that suggest people more likely to produce a conclusion that relates the subject of one premise to the predicate of another
  - More indicative of reasoning process itself

## Mental Models Theory



- Johnson-Laird
- People reason by constructing models
- Conclusions drawn by inspecting models
- If no alternative models refute, draw inference as valid conclusion

## Integrating Premises

- (1) Some of the artists are beekeepers.
- (2) All of the beekeepers are chemists.
- (3) Some of the artists are chemists.

artist =	beekeeper =	chemist
(artist)	(beekeeper) =	chemist
		(chemist)

## Searching for Alternative Models

- (4) All of the artists are beekeepers.
- (5) Some of the beekeepers are chemists.

artist =	beekeeper =	chemist
artist =	beekeeper	(chemist)
	(beekeeper)	

- (6) Some of the artists are chemists. [?]

artist =	beekeeper	
artist =	beekeeper	(chemist)
	beekeeper =	chemist

## What about negatives?

None of the artists is a beekeeper.

artist =	~beekeeper
artist =	~beekeeper
~artist =	beekeeper
~artist =	beekeeper

## Implicit Notation

- Each line shows representative individual w/particular combination of properties
- Dots indicate there may be other types of individuals
- [ ] place restrictions on what properties implicit individuals can have
  - Individuals w/in brackets have been exhaustively represented
- All A are B
  - [a] = b
  - [a] = b
  - ...
- Some A are B
  - a = b
  - a = b
  - ...
- No A are B
  - [a]
  - [a]
  - [b]
  - [b]
  - ...

### Drawing Conclusions

<p>All A are B [a] = b [a] = b ...</p>	<p>All B are C [b] = c [b] = c ...</p>
<p>Combined [[a] = b] = c [[a] = b] = c ...</p>	

### A 3-Model Syllogism

<p>Some B are A No B are C Therefore: Some A are not C. Some B are A b = a b = a ...</p>	<p>No B are C [b] [b] [c] [c] ...</p>
--	---

### First Model

<p>Some B are A b = a b = a ...</p>	<p>No B are C [b] [b] [c] [c] ...</p>			
<p>Combined a = [b] a = [b] ...</p>				
<table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td style="text-align: center;"><u>Potential Conclusions</u></td></tr> <tr><td style="text-align: center;">No A are C</td></tr> <tr><td style="text-align: center;">No C are A</td></tr> </table>		<u>Potential Conclusions</u>	No A are C	No C are A
<u>Potential Conclusions</u>				
No A are C				
No C are A				

### Second Model

<p>Some B are A b = a b = a ...</p>	<p>No B are C [b] [b] [c] [c] ...</p>
<p>Combined a = [b] a = [b] a = [c] [c] ...</p>	

### Second Model

<p>Some B are A b = a b = a ...</p>	<p>No B are C [b] [b] [c] [c] ...</p>					
<p>Combined a = [b] a = [b] a = [c] [c] ...</p>						
<table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td style="text-align: center;"><u>Potential Conclusions</u></td></tr> <tr><td style="text-align: center;">Some A are C</td></tr> <tr><td style="text-align: center;">Some C are A</td></tr> <tr><td style="text-align: center;">Some A are not C</td></tr> <tr><td style="text-align: center;">Some C are not A</td></tr> </table>		<u>Potential Conclusions</u>	Some A are C	Some C are A	Some A are not C	Some C are not A
<u>Potential Conclusions</u>						
Some A are C						
Some C are A						
Some A are not C						
Some C are not A						

### Second Model

<p>Some B are A b = a b = a ...</p>	<p>No B are C [b] [b] [c] [c] ...</p>					
<p>Combined a = [b] a = [b] a = [c] [c] ...</p>						
<table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td style="text-align: center;"><u>Potential Conclusions</u></td></tr> <tr><td style="text-align: center;">Some A are C</td></tr> <tr><td style="text-align: center;">Some C are A</td></tr> <tr><td style="text-align: center;">Some A are not C</td></tr> <tr><td style="text-align: center;">Some C are not A</td></tr> </table>		<u>Potential Conclusions</u>	Some A are C	Some C are A	Some A are not C	Some C are not A
<u>Potential Conclusions</u>						
Some A are C						
Some C are A						
Some A are not C						
Some C are not A						

### Alternative Alternative Model (3<sup>rd</sup>)

Some B are A	No B are C
b = a	[b]
b = a	[b]
...	[c]
	[c]
	...
Combined	
a = [b]	
a = [b]	
a =	[c]
a =	[c]
...	

### Alternative Alternative Model

Some B are A	No B are C
b = a	[b]
b = a	[b]
...	[c]
	[c]
	...
<b>Potential Conclusions</b>	Combined
Some A are C	a = [b]
Some C are A	a = [b]
Some A are not C	a =
*Some C are not A*	[c]
	a =
	[c]
	...

### Common Errors on this Syllogism

- Premise 1: Some B are A  
 Premise 2: No B are C
- All A are C ? (no)
    - Not compatible with any of the models!
  - No C are A ? (yes)
    - Compatible w/1<sup>st</sup> model, but not 2<sup>nd</sup> & 3<sup>rd</sup>
  - No A are C ? (yes)
    - Compatible w/first model, but not 2<sup>nd</sup> & 3<sup>rd</sup>

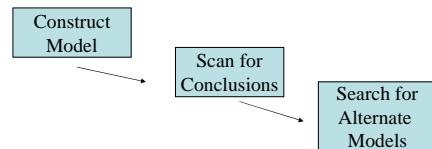
### Evidence for Mental Models Theory

- Problems that require more models are more difficult
  - 3-model problems harder than 2-model problems
  - 2-model problems harder than 1-model problems
- Error patterns suggest people construct some (but not all) mental models

### Mental Models Theory & Wason Selection Task

- If there is a circle, then there is a triangle.
  - [circle] triangle
  - ...
- Modus Tollens requires spelling out the dots: constructing 3 models
  - circle triangle
  - ~circle triangle
  - ~circle ~triangle

### Mental Models Theory Recap



- The more models needed for valid conclusion, the more errors
  - Errors reflect conclusions from initial models