

Conditional Reasoning

Modus Ponens

- (1) $P \rightarrow Q$
- (2) P
- (3) Therefore: Q

Modus Tollens

- (1) $P \rightarrow Q$
- (2) $\sim Q$
- (3) Therefore: $\sim P$

P: John gets B or better on final exam
Q: John passes the course

Invalid Inferences

Denying the Antecedent

- (1) $P \rightarrow Q$
- (2) $\sim P$
- (3) Therefore: $\sim Q$

Affirming the Consequent

- (1) $P \rightarrow Q$
- (2) Q
- (3) Therefore: P

P: The object is square
Q: The object is blue.

Conditional vs. Bi-conditional

P	Q	$P \rightarrow Q$	$P \leftrightarrow Q$
T	T	T	T
T	F	F	F
F	T	T	F
F	F	T	T

If you pick up your toys, I'll read you a story.
If our quarterback is injured, then our team will lose.

Conditional vs. Bi-conditional

P	Q	$P \rightarrow Q$
T	T	T
T	F	F
F	T	T
F	F	T

Affirming the Consequent

- (1) $P \rightarrow Q$
- (2) Q
- (3) Therefore: P

Conditional vs. Bi-conditional

P	Q	$P \rightarrow Q$	$P \leftrightarrow Q$
T	T	T	T
T	F	F	F
F	T	T	F
F	F	T	T

'Affirming the Consequent'

- (1) $P \leftrightarrow Q$
- (2) Q
- (3) Therefore: P

On the biconditional reading of "if", 'Affirming the Consequent' is a valid inference schema!

Conditional vs. Bi-conditional

P	Q	$P \rightarrow Q$
T	T	T
T	F	F
F	T	T
F	F	T

Denying the Antecedent

- (1) $P \rightarrow Q$
- (2) $\sim P$
- (3) Therefore: $\sim Q$

Conditional vs. Bi-conditional

P	Q	$P \rightarrow Q$	$P \leftrightarrow Q$
T	T	T	T
T	F	F	F
F	T	T	F
F	F	T	T

'Denying the Antecedent'
 (1) $P \leftrightarrow Q$
 (2) $\sim P$
 (3) Therefore: $\sim Q$

On the biconditional reading of "if" 'Denying the Antecedent' is a valid inference schema.

Conditional Reasoning in Hypothesis Testing

- Difficulty w/modus tollens inferences seen in performance on hypothesis testing tasks
- Confirmation Bias – tendency to look for evidence that confirms hypothesis rather than falsifying evidence

Wason Selection Task



If a card has a vowel on one side, it has an even number on the other.

- 50% E
- 46% E & 4
- 4% E&7

Wason Selection Task



P	Q	$P \rightarrow Q$
T	T	T
T	F	F
F	T	T
F	F	T

- $P \rightarrow Q$ is always true when Q is true
 - Turning over Q yields no information
- The only time when $P \rightarrow Q$ is false is when P is true and Q is false
 - Need to turn over P to be sure the reverse is Q rather than $\sim Q$
 - Need to turn over $\sim Q$ to be sure the reverse is $\sim P$ rather than P

Poor Performance on the Wason Selection Task

- Matching Hypothesis
- Abstract, Artificial Materials
- Lack of Relevant Experience

Matching Hypothesis

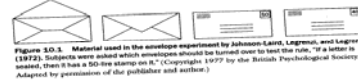
- People link hypothesis to cards by matching the terms in the hypothesis w/cards
- Predicts better performance for
 - A card that has a vowel on one side does NOT have an even number on the other side (shd pick: E&4)
- Predicts worse performance for
 - A card that does NOT have a vowel on one side has an even number on the other side. (shd pick: K&7)



Matching Hypothesis

- Supported by experiments done by Evans and colleagues
 - Matching at least part of the story...
- Why do people do this? Evans speculates
 - People assume the terms mentioned in the problem will be relevant to the solution
 - Because people find it difficult to reason with negative statements, they ignore them

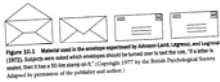
Concrete vs. Artificial Materials



If a letter is sealed, it has a 50 lire stamp on the other side.

- Johnson-Laird, Legrenzi, & Legrenzi
- 22/24 Correct (compared with 2/24 on Wason's original study)

Envelope Version of WST



- Do concrete materials make task easier?
- Griggs & Cox
 - American college students had trouble w/the envelopes
- Golding
 - Brits under 45 had trouble
 - Brits over 45 did not

Relevant Experience

- If a person is drinking beer, then the person must be over 21 years of age



- Performance on WST enhanced when thematic material cues retrieval of directly experienced knowledge in LTM

Pragmatic Reasoning Schemas



- Permission, Obligation, Authorization concepts organize conditional reasoning
- Reasoning schemas aren't completely abstract forms that are independent of their contents
 - Use schemas for permission, obligation, and authorization
- Thematic material triggers particular schemas
 - Anyone consuming Pepsi on these premises must be at least 100 years old.
 - Any lengths of red wool must be at least 6 meters long.

Cheng & Holyoak

Two Interpretations of Content Effects

- ⊗ People have limited (or no) abstract reasoning abilities
 - They use frames and schemas instead
- ☺ People can reason abstractly, but their ability to link concrete information to abstract schemas depends on the content
 - That is, $A \rightarrow B, B \rightarrow C, \therefore A \rightarrow C$
 - How to decide A, B, C instantiated in real world cases
 - Is B the same in Premise 1 and Premise 2 (J. Edgar Hoover example)

Syllogistic Reasoning

- Aristotle first developed formal logic
 - Syllogistic reasoning
- Categorical Syllogisms
 - All men are mortal.
 - Socrates is a man.
 - Therefore: Socrates is mortal.
- Concrete as well as Abstract Instantiations
 - All A's are B's.
 - All B's are C's.
 - Therefore: All A's are C's.

Some A's are B's

- Some A's are B's.
Some B's are C's.
Therefore: Some A's are C's. (INVALID)
- Some men are philosophers.
Some philosophers are women.
Therefore: Some men are women. (INVALID)

Atmosphere Effects

- Finding that people are more prone to accept arguments as valid if quantifiers in premises and conclusions are the same.
- Sometimes this works:
 - All A's are B's.
 - All B's are C's.
 - Therefore: All A's are C's.
- Sometimes it doesn't work:

No A's are B's.	No women are robots.
No B's are C's.	No robots are ballerinas.
Therefore: No A's are C's.	No women are ballerinas.

Woodworth & Sells, 1935

Atmosphere Hypothesis

- Negative premise creates a negative atmosphere
 - Negative Conclusion
- Particular premise (some) creates a particular atmosphere
 - Particular Conclusion
- Valid > Invalid
 - Reflects reasoning processes

Evidence against the Atmosphere Hypothesis

- Most evidence consistent w/AH
- But:
 - Some B are A.
 - No C are B.
 - Therefore: Some A are not C.
 (Only 10% of people offer this conclusion, while 60% say there is no valid conclusion.)

Conversion Hypothesis

- Syllogistic reasoning errors result because people reinterpret premises
 - All A's are B's \Rightarrow All B's are A's
 - Some A's are not B's \Rightarrow Some B's are not A's
- Predicts:
 - All A's are B's.
 - Some C's are B's.
 - Therefore: Some C's are A's. (INVALID) (People do make this error.)
 A=ocean liners B=vehicles C=toys

Support for Conversion Hypothesis

- Restate premises in less ambiguous form
 - Performance improves!
- All A's are B's, but some B's are not A's.
 Some C's are B's.
 Some C's are A's. ← INVALID (and everyone knows it!)

Belief Bias Effect

- Tendency to accept arguments with a true conclusion as being valid

All things that have motors need oil.
 Automobiles need oil.
 Therefore: Automobiles have motors. (INVALID)

All things that have motors need oil.
 Wombats need oil.
 Therefore: Wombats have motors. (INVALID)

Syllogistic Reasoning Errors

- Atmosphere Effects
 - Superficial Processing
- Conversion Effects
 - Comprehension Problems
- Belief Bias
 - Intrusion of Prior Beliefs
- Figural Effects
 - Findings that suggest people more likely to produce a conclusion that relates the subject of one premise to the predicate of another
 - More indicative of reasoning process itself

Figural Effects

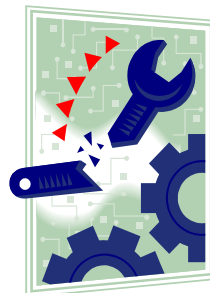
- Example
 - Some artists are beekeepers.
 - All of the beekeepers are chemists.
 - Therefore: Some of the artists are chemists.
 - Therefore: Some of the chemists are artists.
- More natural to go from subject of one premise to predicate of the other in formulating a conclusion



Potential Errors

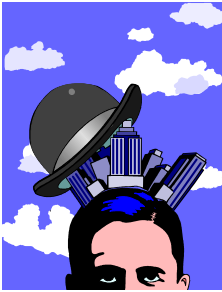
- Figural effects also lead to errors
 - All of the beekeepers are artists.
 - None of the chemists are beekeepers.
 - Some of the artists are not chemists. (VALID)
 - Some of the chemists are not artists. (INVALID)
- BA
 CB
 CA (Figural Effect)
 AC (Contra-Figural Effect)

Processing Limitations



- Internal Consistency Check
- Failure to Consider All Possible Instantiations of Premises

Mental Models Theory



- Johnson-Laird
- People reason by constructing models
- Conclusions drawn by inspecting models
- If no alternative models refute, draw inference as valid conclusion

Mental Models Theory

- The lamp is on the right of the pad. pad lamp
- The book is on the left of the pad. book pad lamp
- The clock is in front of the book. book pad lamp clock
- The vase is in front of the lamp. book pad lamp clock vase

Multiple Models

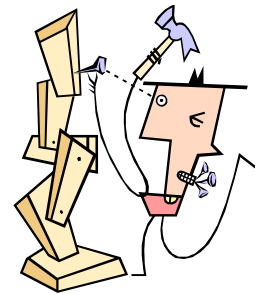
- The lamp is on the right of the pad.
- The book is on the left of the lamp.
- The clock is in front of the book.
- The vase is in front of the pad.

book pad lamp
clock vase

pad book lamp
vase clock

Mental Models Theory

- 3 Stages
 - Comprehension of Premises
 - Formulate Conclusion
 - Search for Alternative Models
- Models
 - Specific
 - Analogue
 - Visual Images OR Unconscious



More Mental Models Theory

- Procedures
 - Conclusion-forming
 - Revision
- Errors caused by WM Limitations
 - More models needed, more errors likely

Syllogistic Reasoning & Mental Models Theory

(1) Some of the artists are beekeepers.

artist = beekeeper
(artist) (beekeeper)

artist = beekeeper
artist = beekeeper
(artist) (beekeeper)

All of the beekeepers...

(2) All of the beekeepers are chemists.

beekeeper =	chemist
beekeeper =	chemist
	(chemist)

Integrating Premises

(1) Some of the artists are beekeepers.

(2) All of the beekeepers are chemists.

(3) Some of the artists are chemists.

artist =	beekeeper =	chemist
(artist)	(beekeeper) =	chemist
		(chemist)